

**Revision Booster  
WORKSHOP  
for  
NEET & JEE Main**

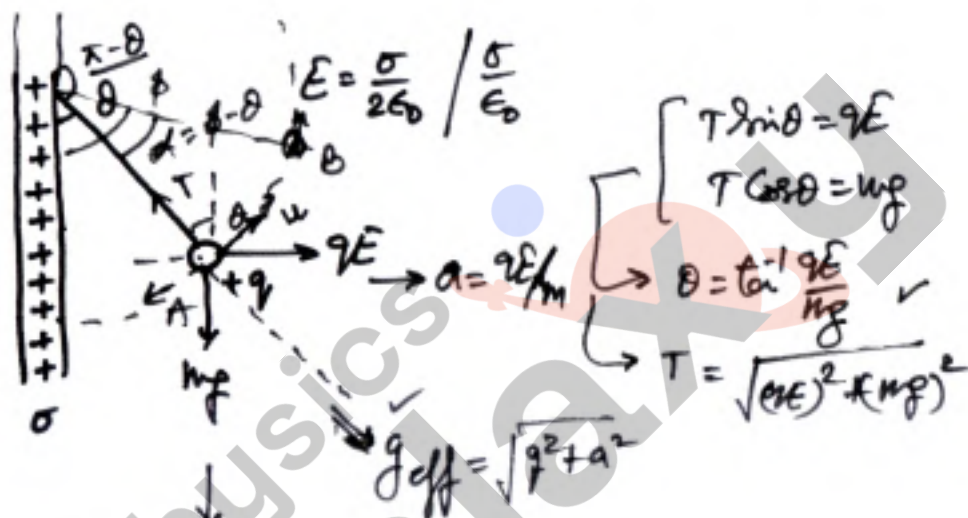
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**Electrostatics &  
Gravitation**

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Notes of Revision Booster Workshop for JEE Main & NEET  
**9000+ Classes available on PHYSICS GALAXY Mobile app**

QUESTIONS BASED ON  
**# EQUILIBRIUM OF A BOB HANGING FROM A CHARGED SHEET**



Osc period

$$T = 2\pi \sqrt{\frac{l}{g_{\text{eff}}}}$$

W/E theorem from A to B

QUESTIONS BASED ON  
**# OIL DROP IN MILLIKAN EXPERIMENT**

for eq<sup>m</sup> of drop

$$\frac{q\sigma}{\epsilon_0} = mg$$

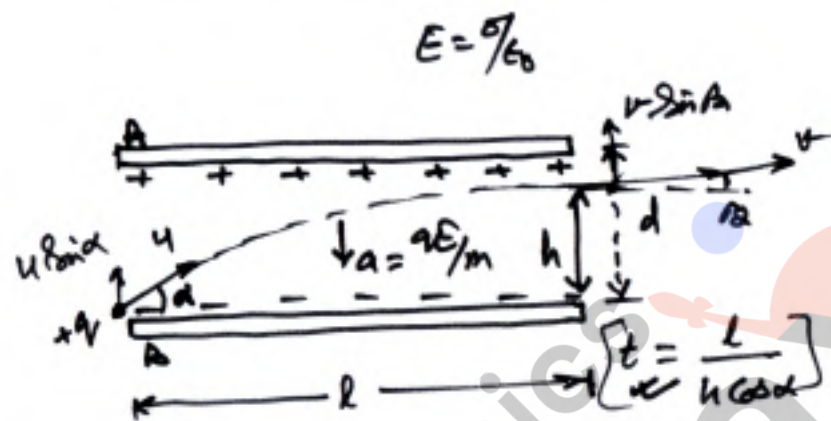
$$q = n e$$

if drop is moving at T. speed

at T. speed

$$[qE + 6\pi\eta r v = \frac{4}{3}\pi r^3 \rho \cdot g]$$

QUESTIONS BASED ON  
**# PROJECTILE INSIDE A CAPACITOR**

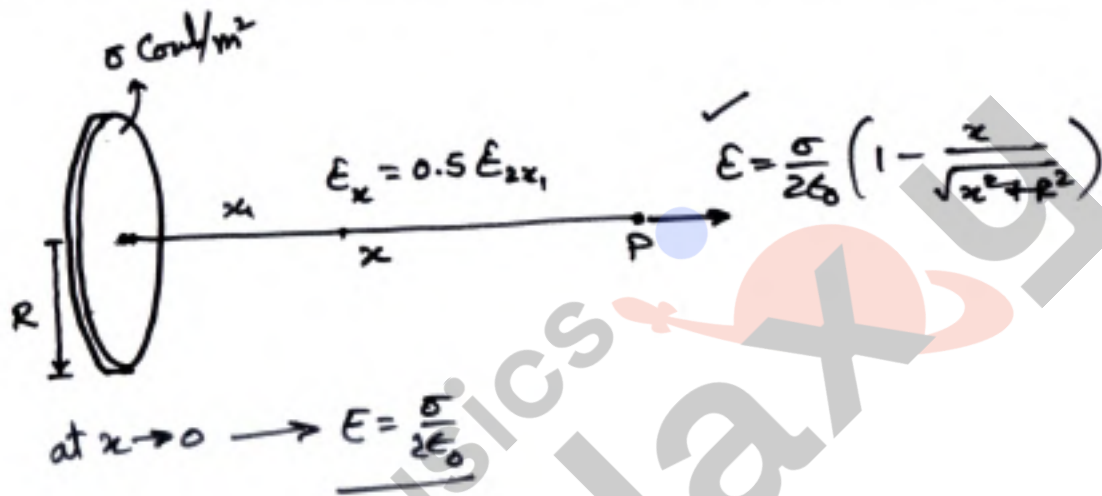


$$\left[ \begin{array}{l} u \cos \alpha = v \cos A \\ v \sin A = u \sin \alpha - gt \end{array} \right]$$

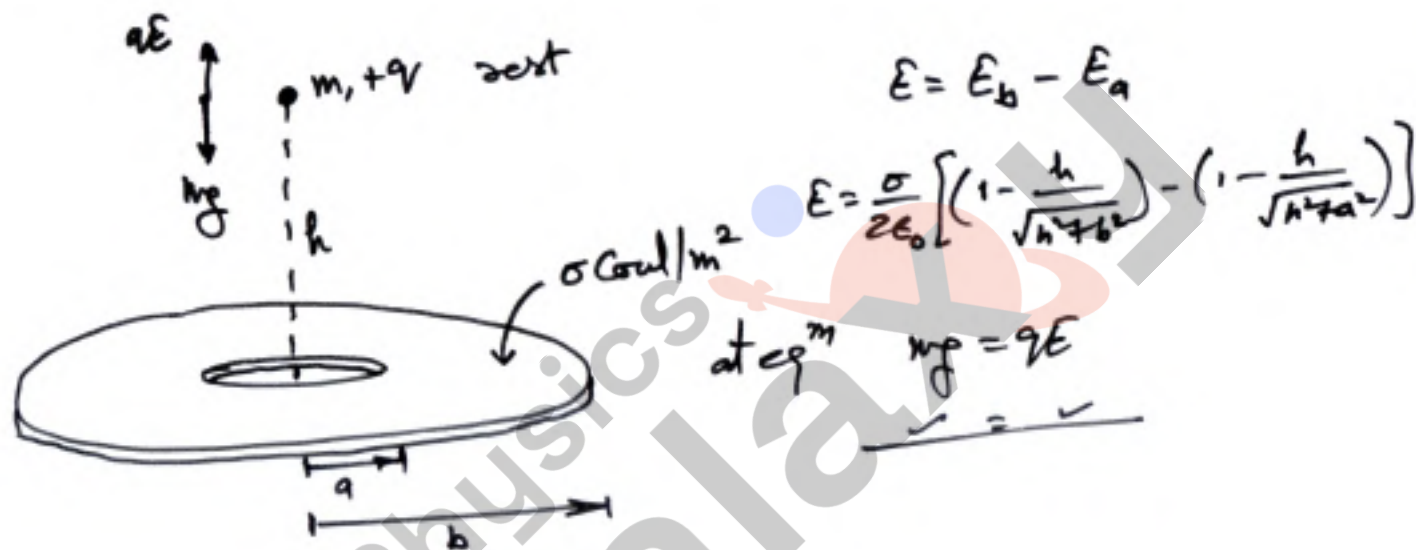
$$a = \frac{q\sigma}{m\epsilon_0}$$

$$h = u \sin \alpha t - \frac{1}{2} a t^2$$

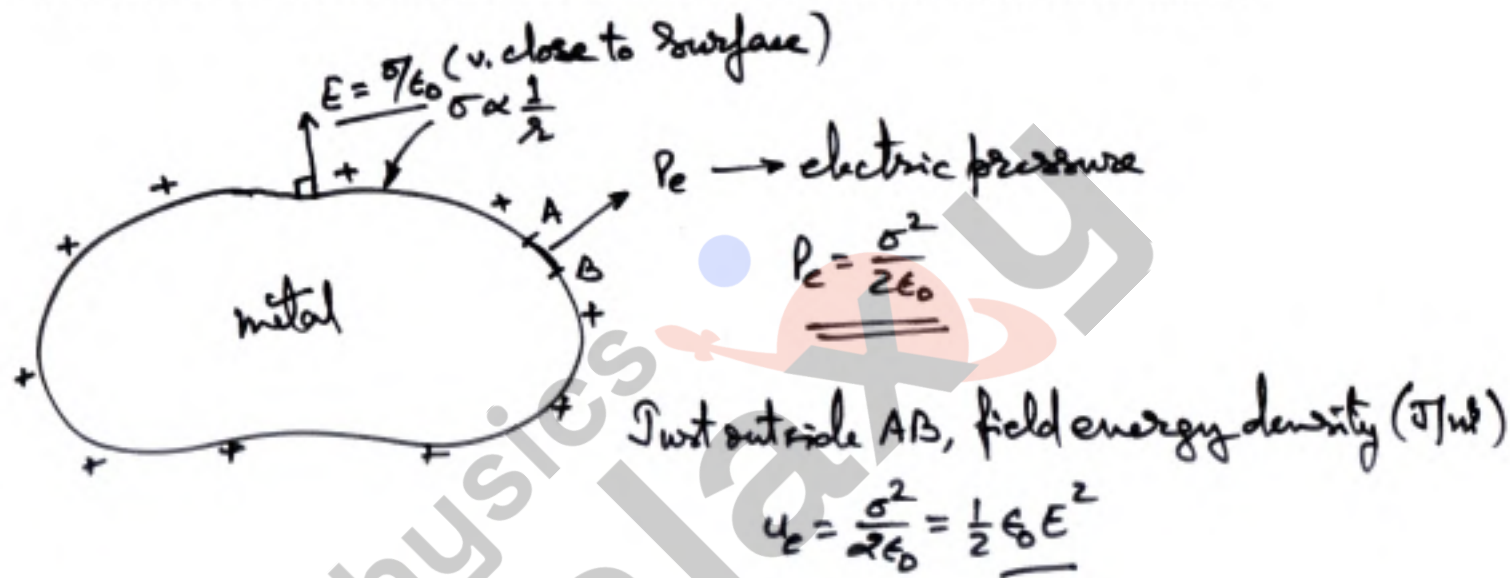
QUESTIONS BASED ON  
**# ELECTRIC FIELD VARIATION ALONG AXIS OF A DISC**



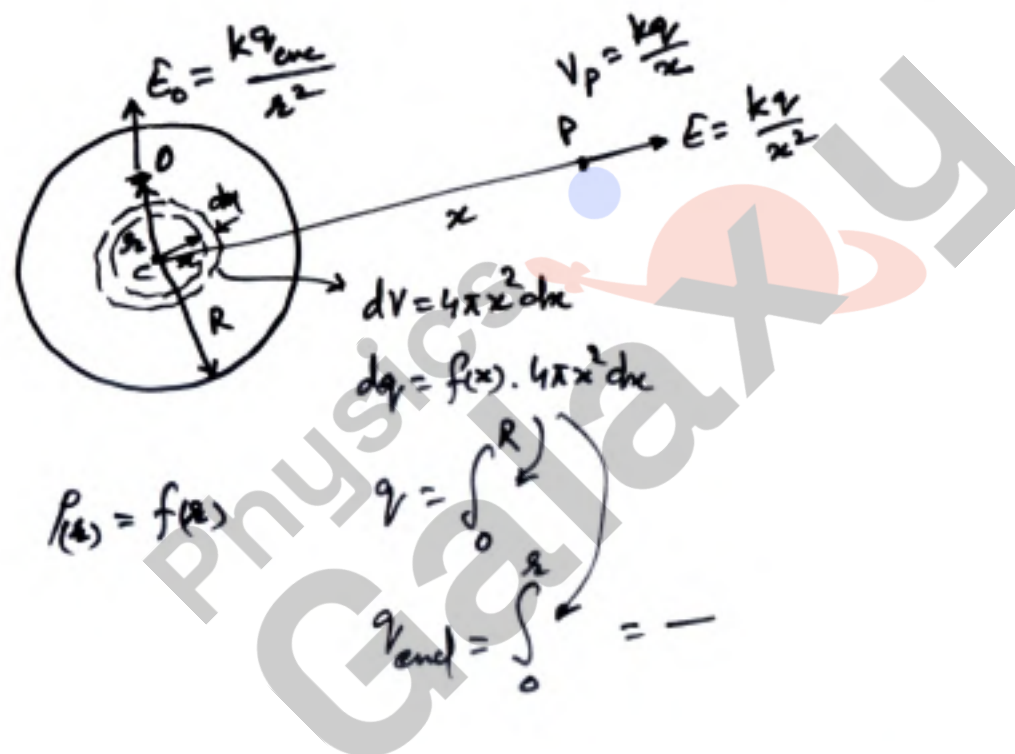
QUESTIONS BASED ON  
**# PARTICLE IN EQUILIBRIUM OVER AN ANNULAR DISC**



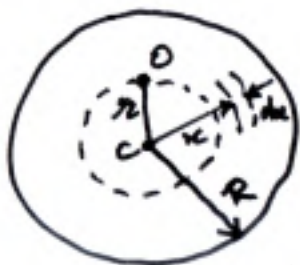
QUESTIONS BASED ON  
# ELECTRIC FIELD JUST OUTSIDE A CHARGED CONDUCTOR



QUESTIONS BASED ON  
**# ELECTRIC FIELD & POTENTIAL DUE TO SPHERICAL CHARGE DISTRIBUTION**



QUESTIONS BASED ON  
**# ELECTRIC POTENTIAL INSIDE A SPHERICAL CHARGE DISTRIBUTIONS**

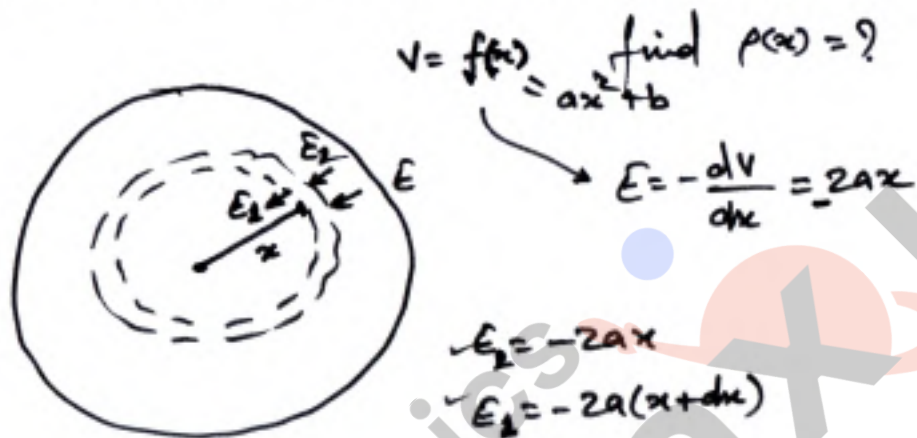


$$V_0 = \int_{\infty}^R |\vec{E}_{out} \cdot d\vec{r}| + \int_R^r |\vec{E}_{in} \cdot d\vec{r}|$$

OR

$$V_0 = \left[ \frac{K q_{enc}}{r} + \int_r^R \frac{(f(x) \cdot 4\pi x^2 dx) K}{x} \right]$$

QUESTIONS BASED ON  
**# CALCULATION OF CHARGE DISTRIBUTION**

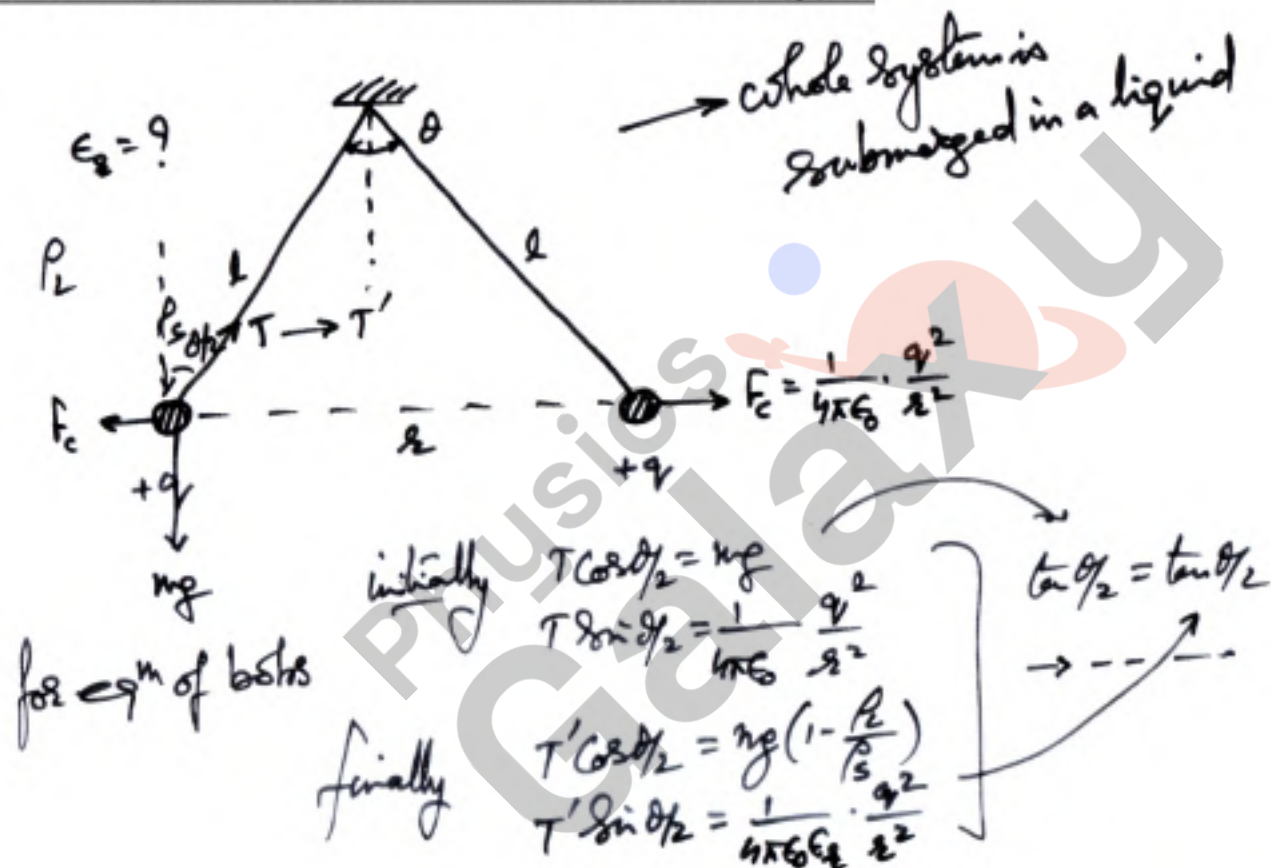


From Gauss's law on elemental shell, we get

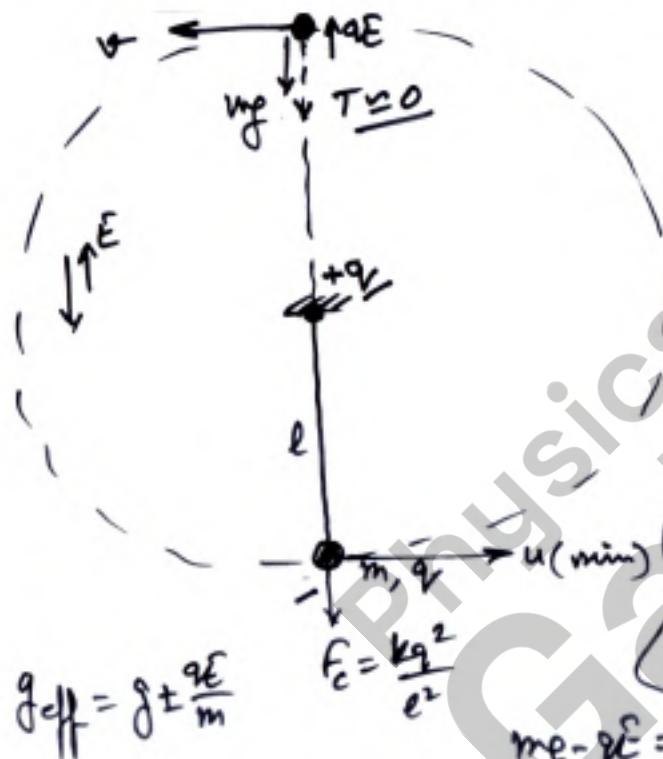
$$E_2(4\pi(x+dx)^2) - E_1(4\pi x^2) = \frac{dq}{\epsilon_0} = \rho(x) \cdot 4\pi x^2 dx$$

$$\rho(x) = \underline{\hspace{2cm}}$$

QUESTIONS BASED ON  
**# PENDULUMS SUBMERGING IN A LIQUID**



QUESTIONS BASED ON  
**# VERTICAL CIRCULAR MOTION WITH CHARGES IN EF**



In presence of EF  $u_{\text{min}} = \sqrt{5g_{\text{eff}}l}$ .

In presence of +ve at suspension pt  
 at topmost point speed of bob

$$v = \sqrt{u^2 - 4gl}$$

At topmost pt, we use

for  $u_{\text{min}}$  -

$$mg - qE = \frac{mv^2}{l}$$

$u =$   $\rightarrow$  Ans

$$g_{\text{eff}} = g \pm \frac{qE}{m}$$

QUESTIONS BASED ON  
# A CHARGE MOVING IN NON-UNIFORM EF

$v_i = 0$   
 $m$   
 $+q$

$x$   $\rightarrow$   $E = f(x)$   $\rightarrow$   $y$   $\rightarrow v$

$\rightarrow a = \frac{qE}{m}$

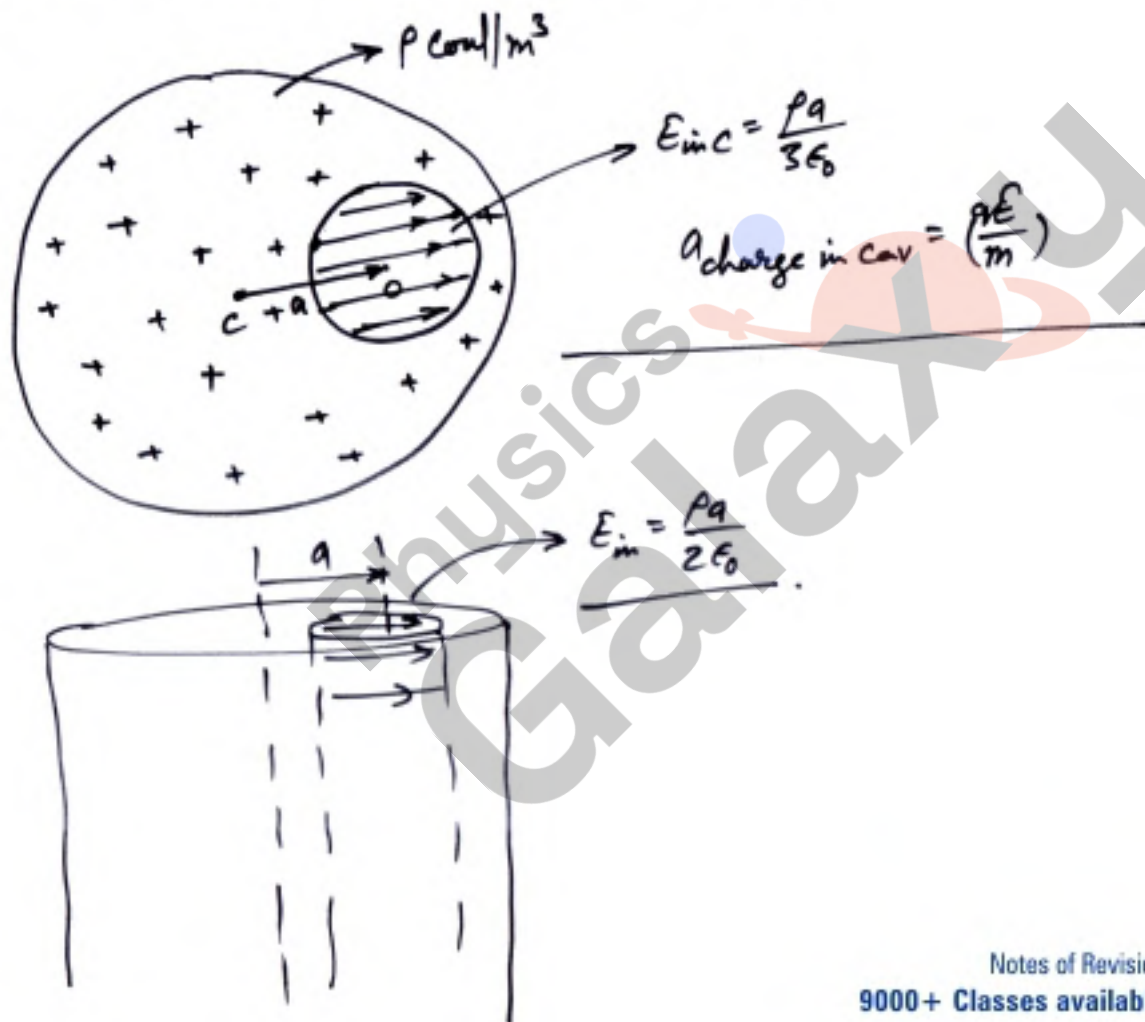
$v \frac{dv}{dx} = \frac{qE_x}{m}$

$\int_0^v v dv = \int_0^x \frac{qE_x}{m} dx$

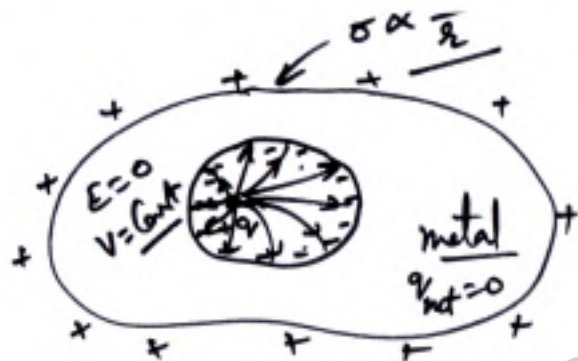
$v_x - v_y = \left| \int_0^x E_x dx \right|$

W/E theorem  $\Rightarrow q(v_x - v_y) = \frac{1}{2}mv^2$

QUESTIONS BASED ON  
# MOTION OF A CHARGE INSIDE CAVITY



QUESTIONS BASED ON  
**# INDUCED CHARGES INSIDE METAL CAVITIES**



flux from a pt charge

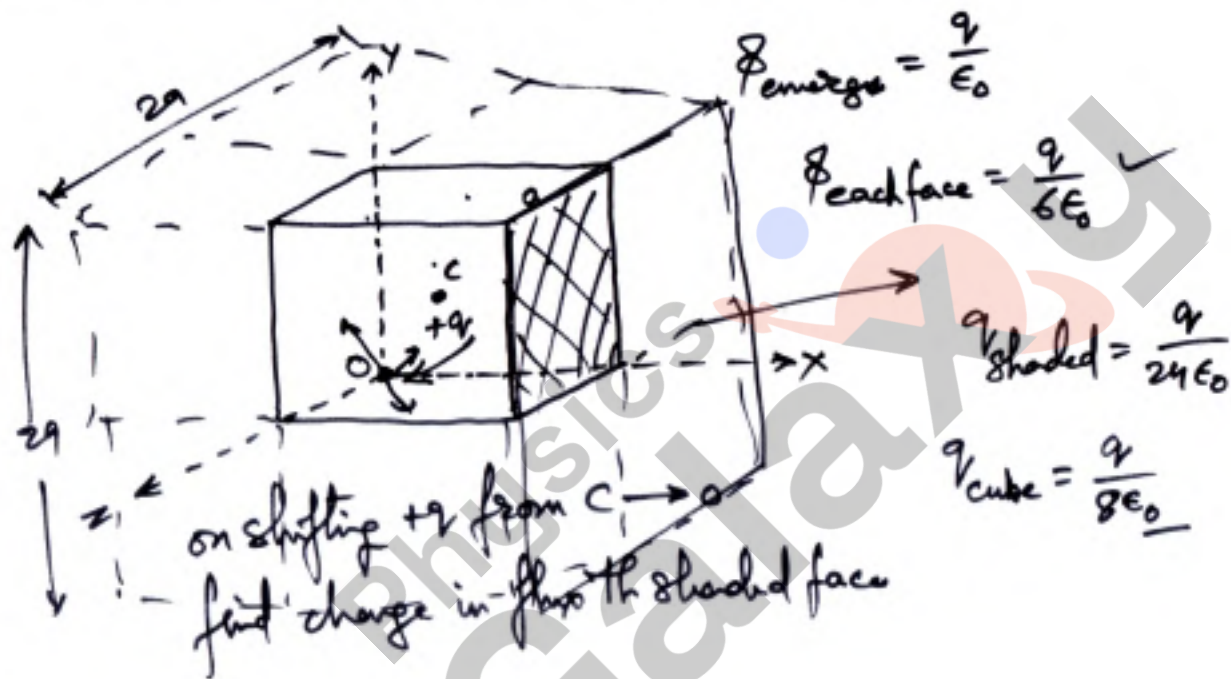
$$\Phi = \frac{q}{\epsilon_0}$$

out of induced surface charges on cavity  
 inner surfaces

$$q_{in} = -q$$

Surface of cavity close to pt charge  
 has higher value of  $\sigma_i$  ( $\propto \frac{1}{r^2}$ )

QUESTIONS BASED ON  
**# ELECTRIC FLUX FROM A CUBICAL SURFACE**



QUESTIONS BASED ON  
**# CHARGE ENCLOSED IN A CUBE IN VARYING ELECTRIC FIELD**

$$E = f(x) = C_1 x^2 + C_2$$

$$\phi_{in} = (C_1 a^2 + C_2) \cdot a^2$$

$$\phi_{out} = (C_1 (4a^2) + C_2) a^2$$

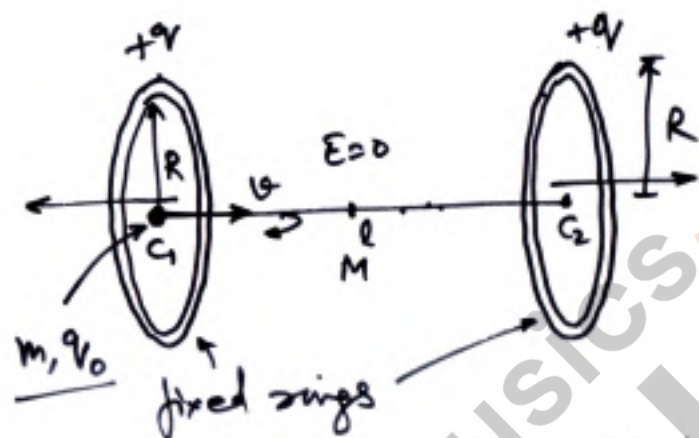
$$\phi_{out} - \phi_{in} = \frac{q_{enc}}{\epsilon_0}$$

$$q_{enc} = \dots \checkmark$$

$$area = a^2$$

$$q_{enc} = ?$$

QUESTIONS BASED ON  
**# THROWING OF A PARTICLE BETWEEN RING CENTERS**



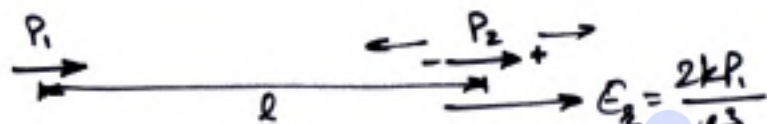
if KE reqd to cross null pt is  $K = \frac{1}{2} m v_{\min}^2$

$$\Rightarrow K \geq q (V_M - V_{C_1})$$

$$\frac{1}{2} m v_{\min}^2 = q \left[ \frac{2 k q}{\sqrt{R^2 + (l/2)^2}} - \left( \frac{kq}{R} + \frac{kq}{\sqrt{l^2 + R^2}} \right) \right]$$

$$v_{\min} = \dots$$

QUESTIONS BASED ON  
**# FORCE BETWEEN TWO DIPOLES**



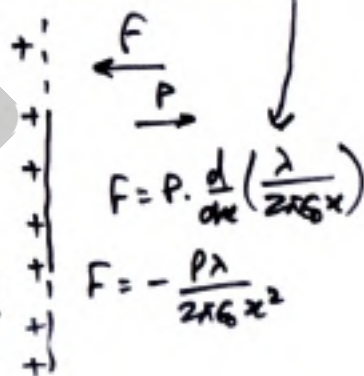
force on  $P_2$  is given as

$$F = P_2 \frac{2kP_1}{l^3} \times 3 = \frac{6kP_1 P_2}{l^4} \quad (\text{attractive})$$

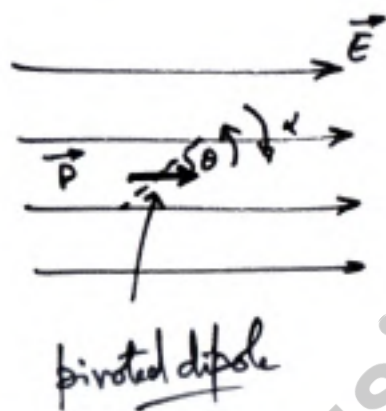
$$\vec{F} = -\frac{dU}{dx} \hat{i} \quad \text{and} \quad U = -\vec{P} \cdot \vec{E}$$

$$\vec{F} = \left( \vec{P} \cdot \frac{d\vec{E}}{dx} \right) \hat{i}$$

force on a dipole  $F = + \vec{P} \cdot \frac{d\vec{E}}{dx}$



QUESTIONS BASED ON  
**# OSCILLATION OF A DIPOLE IN EXTERNAL EF**



if dipole is slightly rotated, restoring torque on dipole

$$\vec{\tau} = \vec{p} \times \vec{E}$$

$$\tau_R = PE \sin \theta$$

for small  $\theta$   $\tau_R = PE \theta$

$$I \alpha = PE \theta$$

$$\alpha = -\frac{PE}{I} \theta$$

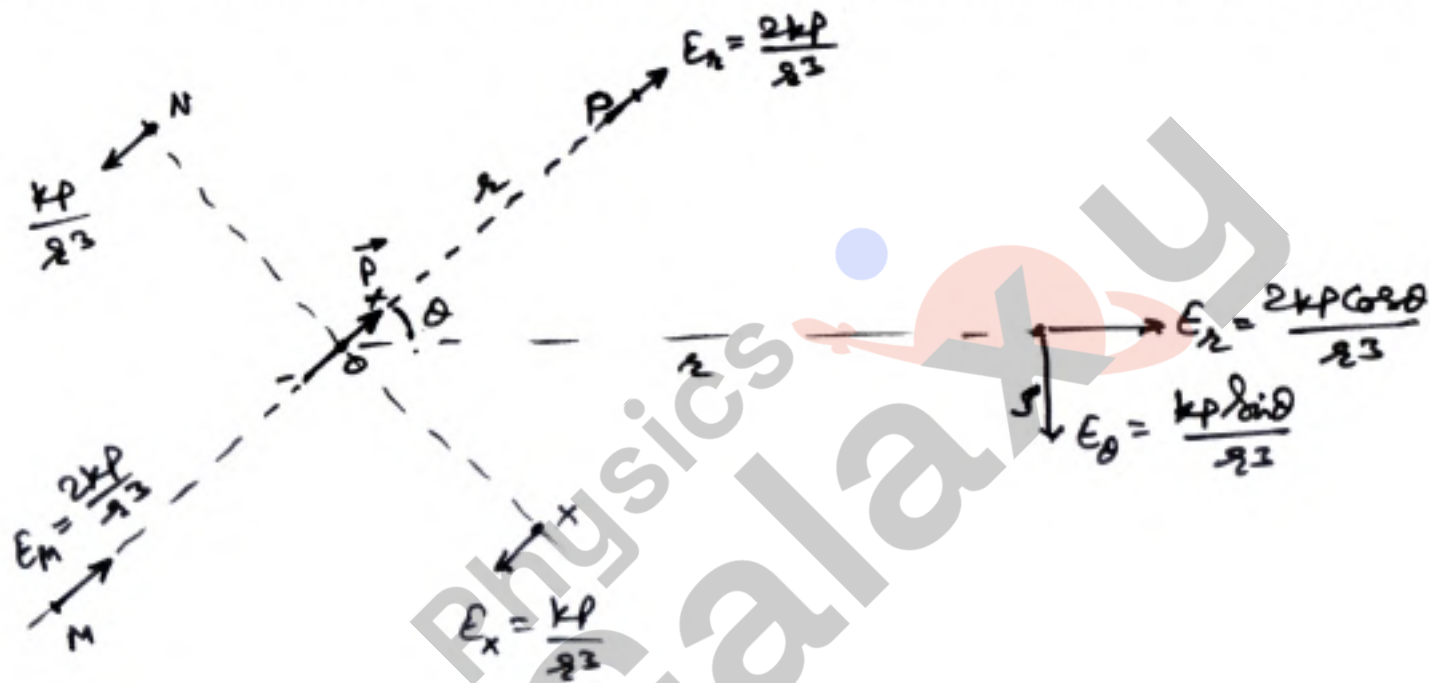
Comp with

$$\alpha = -\omega^2 \theta$$

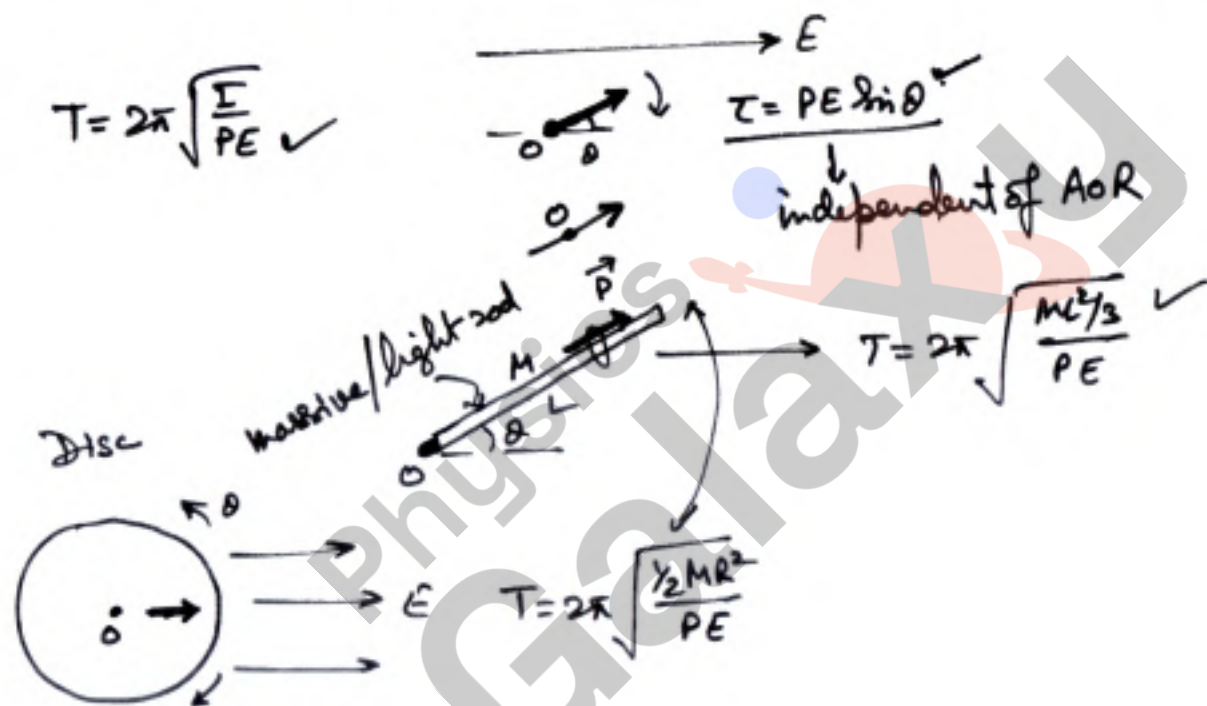
$$\omega = \sqrt{\frac{PE}{I}}$$

$$T = \frac{2\pi}{\omega} = 2\pi \sqrt{\frac{I}{PE}}$$

QUESTIONS BASED ON  
**# DIRECTIONS OF RADIAL & TRANSVERSE FIELD DUE TO A DIPOLE**

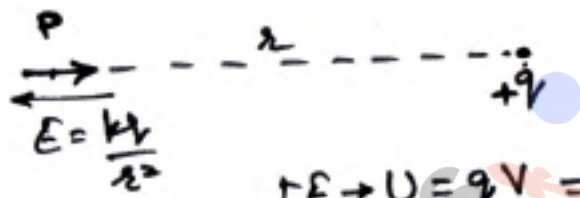


QUESTIONS BASED ON  
**# OSCILLATION OF BODIES IN ELECTRIC FIELD WITH A DIPOLE**



QUESTIONS BASED ON  
**# POTENTIAL ENERGY OF A POINT CHARGE & DIPOLE**

due to the  
Interaction  
 bet<sup>w</sup>  $q$  &  $P$

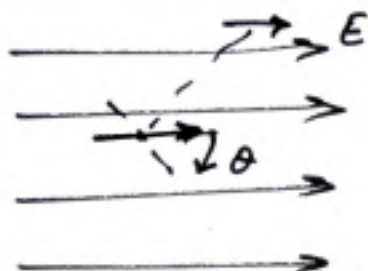


$$\int E_q \rightarrow U = qV = q \left( \frac{kq}{r^2} \right) = \frac{kq^2 P}{r^2} \checkmark$$

$$\int E_p \rightarrow U = -PE \cos \theta = -P \left( \frac{kq}{r^2} \right) \cos 180^\circ = \frac{kqP}{r^2} \checkmark$$



QUESTIONS BASED ON  
**# WORK DONE IN MOVING A DIPOLE**



$$U_i = -PE$$

$$U_f = -PE \cos \theta$$

initial PE  $\rightarrow U_i$   
 final PE  $\rightarrow U_f$

$$W_{\text{ext}} = U_f - U_i$$

$$W_{\text{sys}} = U_i - U_f$$

$$W_{\text{ext}} = PE(1 - \cos \theta)$$

$$W_{\text{field}} = PE(\cos \theta - 1)$$

NOTE: if dipole orientation  
 is not changing in motion

$$\underline{W = 0}$$

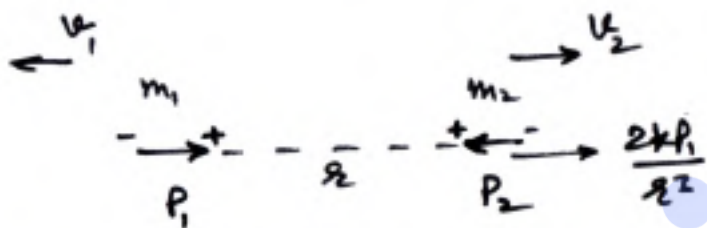
if  $I$  is MI of dipole, we can use

$$W_{\text{ext}} = \frac{1}{2} I \omega^2 \rightarrow \omega = \dots$$

QUESTIONS BASED ON  
**# WORK IN DISPLACING A DIPOLE IN SURROUNDING OF A CHARGE**

$U_f' = 0$   
 $W = 0 - \left(-\frac{kpq}{r^2}\right) = \frac{kpq}{r^2}$   
 $U = -PE \cos \theta$   
 $U_i = -P \left(\frac{kq}{r^2}\right) = U_f$   
 $W_{ext} = 0$   
 $U_f = -P \left(\frac{kq}{r^2}\right) \cos \theta \Rightarrow W_{ext} = U_f - U_i = -$

QUESTIONS BASED ON  
**# KINETIC ENERGY IN REPELLING DIPOLES**



find KE of  $P_1$  and  $P_2$  when sep increased to  $2r$

$$U_i = \frac{2kp_1p_2}{r^3}$$

$$U_f = \frac{2kp_1p_2}{8r^3} = \frac{kp_1p_2}{4r^3}$$

finally

$$U_i - U_f = \frac{1}{2}m_1v_1^2 + \frac{1}{2}m_2v_2^2$$

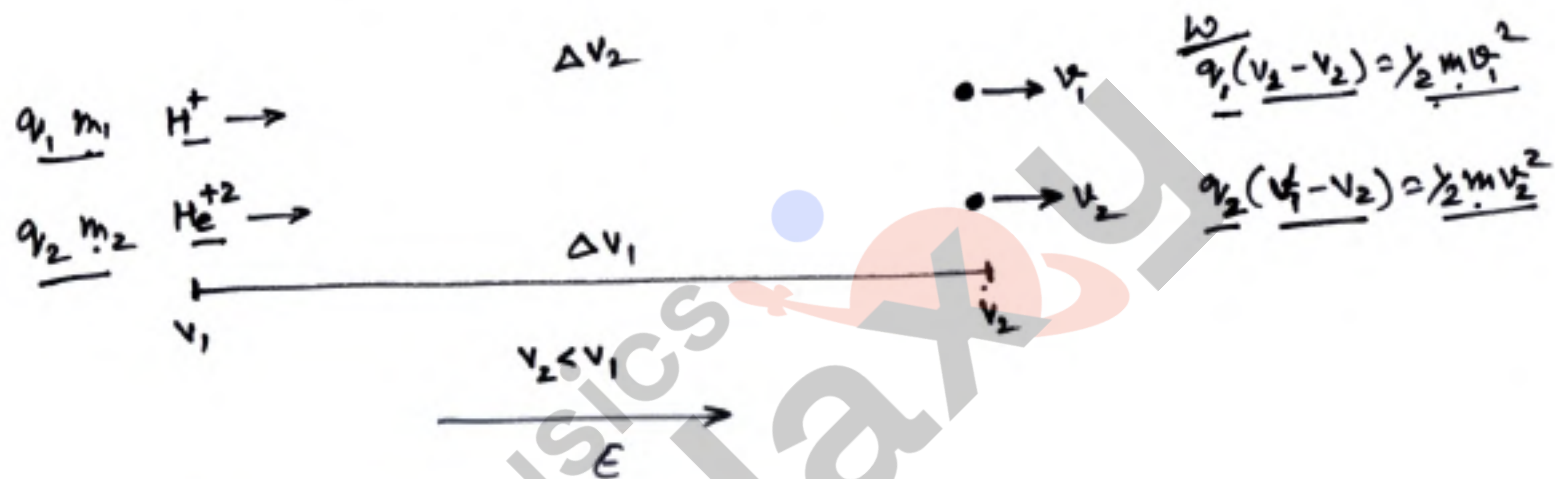
$$m_1v_1 = m_2v_2$$

$$v_1 = \text{---}$$

$$v_2 = \text{---}$$

QUESTIONS BASED ON

## # TWO IONS ACCELERATED BY SAME POTENTIAL DIFFERENCE



$$W = q \Delta V.$$

if final KE are same then we use

$$q_1 \Delta V_1 = q_2 \Delta V_2 \rightarrow \left[ \frac{q_1}{q_2} = \frac{\Delta V_2}{\Delta V_1} \right]$$

QUESTIONS BASED ON  
**# WORK DONE BY A LINE CHARGE ON POINT CHARGE**

The diagram shows a vertical line charge with linear charge density  $\lambda$  (Coul/m) on the left. A point charge  $+q$  is shown at two positions,  $r_1$  and  $r_2$ , from the line charge. A dashed line connects the two positions, with velocity vectors  $v_1$  and  $v_2 = v$  indicating motion from  $r_1$  to  $r_2$ .

Equations for potential difference and work done:

$$V_1 - V_2 = \int_{r_1}^{r_2} E \cdot dr = \int_{r_1}^{r_2} \frac{\lambda}{2\pi\epsilon_0 x} \cdot dx$$

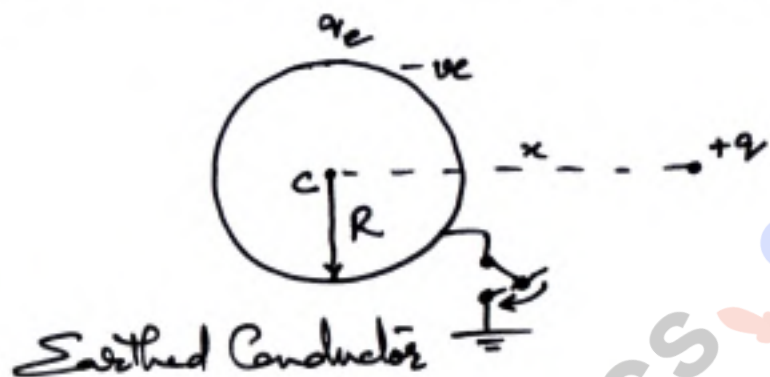
$$V_1 - V_2 = \frac{\lambda}{2\pi\epsilon_0} \ln\left(\frac{r_2}{r_1}\right)$$

Work done  $W = \Delta K$

$$q(V_1 - V_2) = \frac{1}{2} m (v_2^2 - v_1^2)$$

$$\frac{q\lambda}{2\pi\epsilon_0} \ln \frac{r_2}{r_1} = \frac{1}{2} m (v_2^2 - v_1^2)$$

QUESTIONS BASED ON  
**# EARTHING OF SPHERICAL SHELLS**

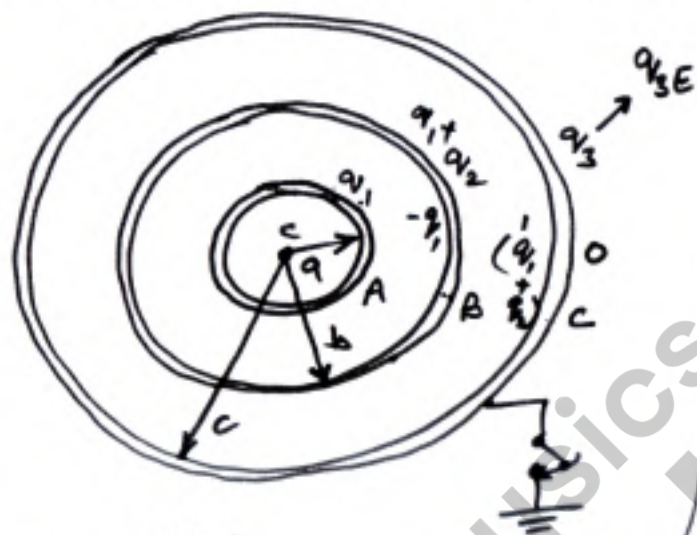


$$V_f = 0$$

$$\frac{kq}{x} + \frac{kq_e}{R} = 0$$

$$q_e = -\frac{qR}{x}$$

QUESTIONS BASED ON  
**# EARTHING OF CONCENTRIC SHELLS**



$$V_A = \frac{kq_1}{a} + \frac{kq_2}{b} + \frac{kq_3}{c}$$

$$V_B = \frac{kq_1}{b} + \frac{kq_2}{b} + \frac{kq_3}{c}$$

$$V_C = \frac{k(q_1 + q_2 + q_3)}{c}$$

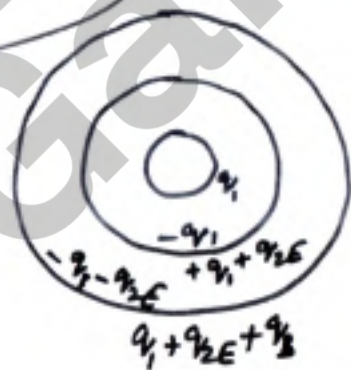
$$V_{C=0} = \frac{k(q_1 + q_2 + q_{3E})}{c} = 0$$

$$q_{3E} = -\frac{(q_1 + q_2)}{1} \checkmark$$

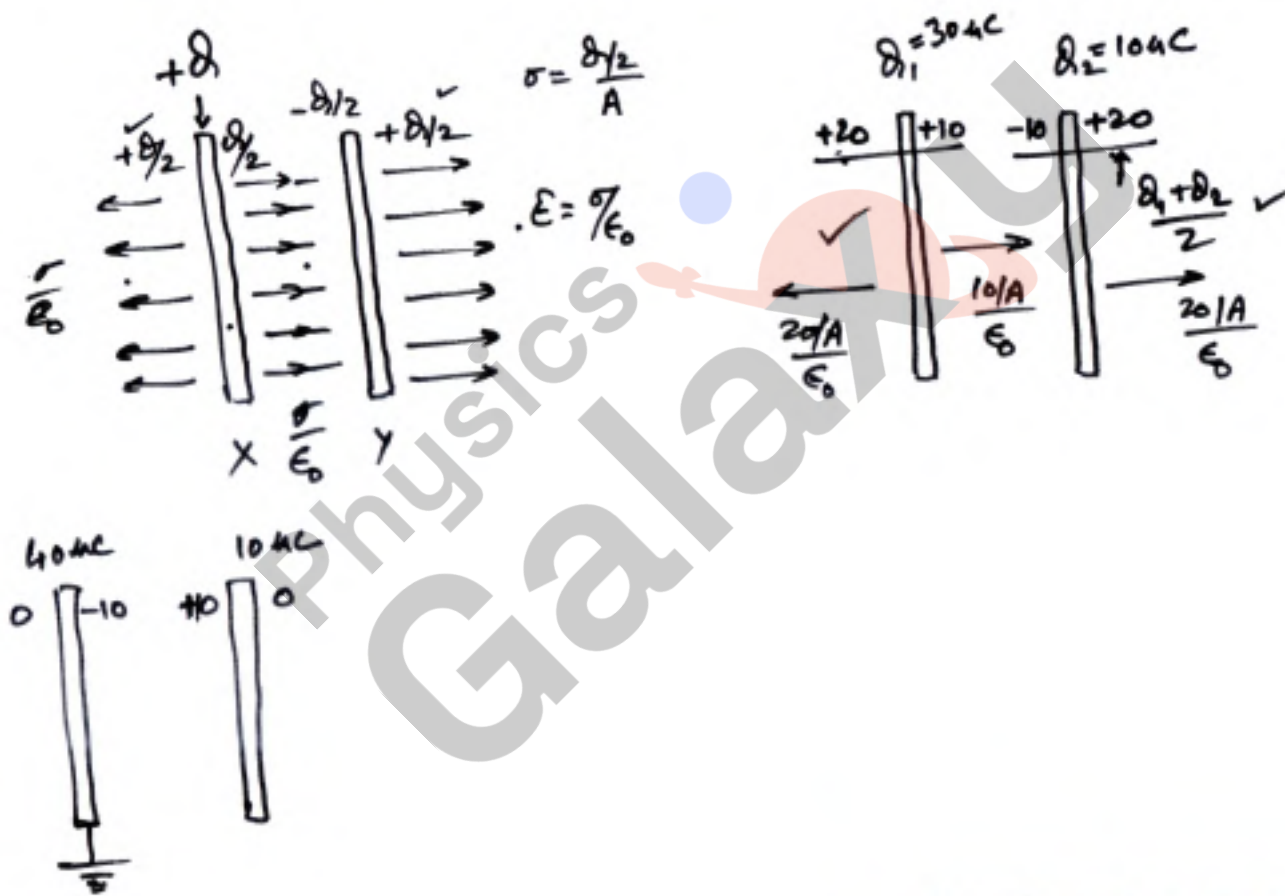
if B is earthed

$$\frac{q_1 + q_2 E}{b} + \frac{q_3}{c} = 0$$

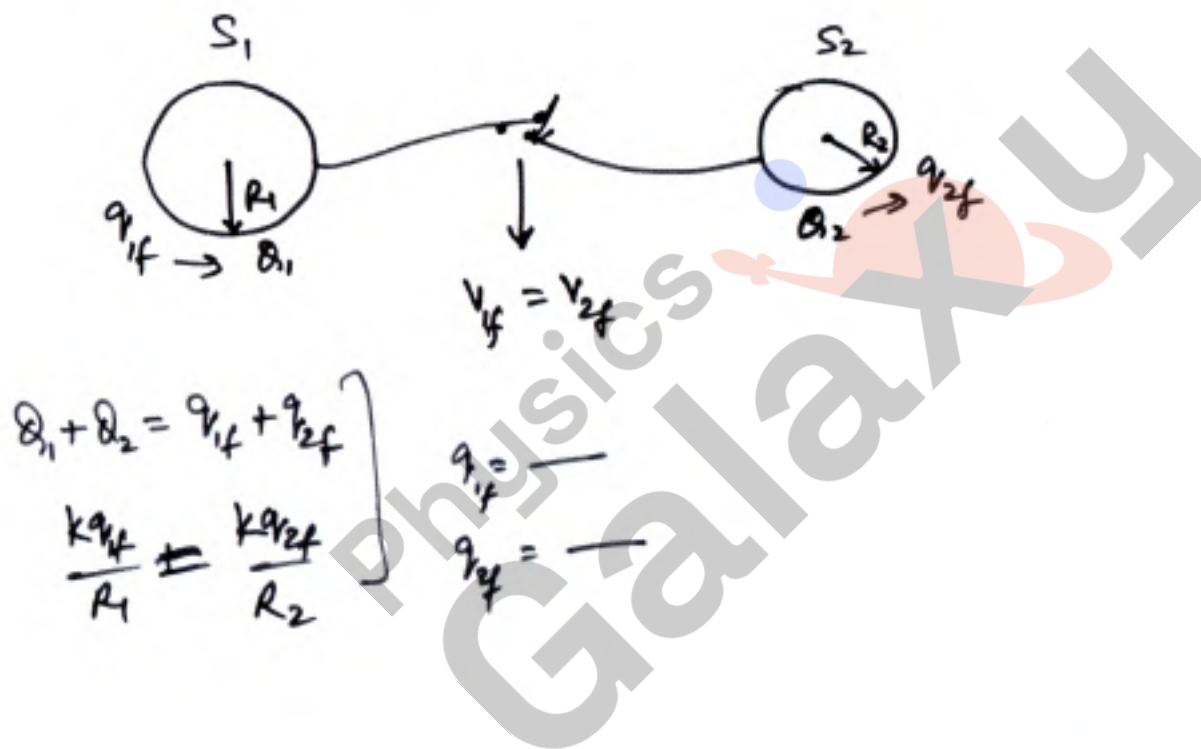
$$q_2 E = b \left[ \frac{q_3}{c} + \frac{q_1}{b} \right]$$



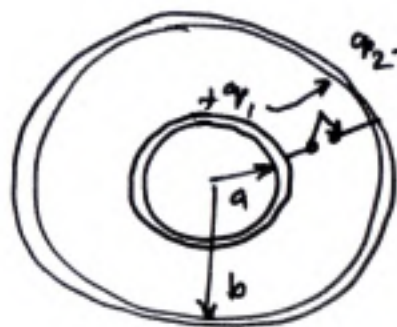
QUESTIONS BASED ON  
**# CHARGE DISTRIBUTION & FIELD CONFIGURATION IN PARALLEL PLATES**



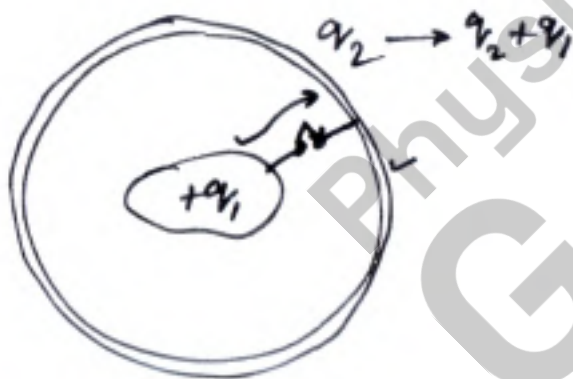
QUESTIONS BASED ON  
**# CONNECTING TWO CONDUCTING SPHERES**



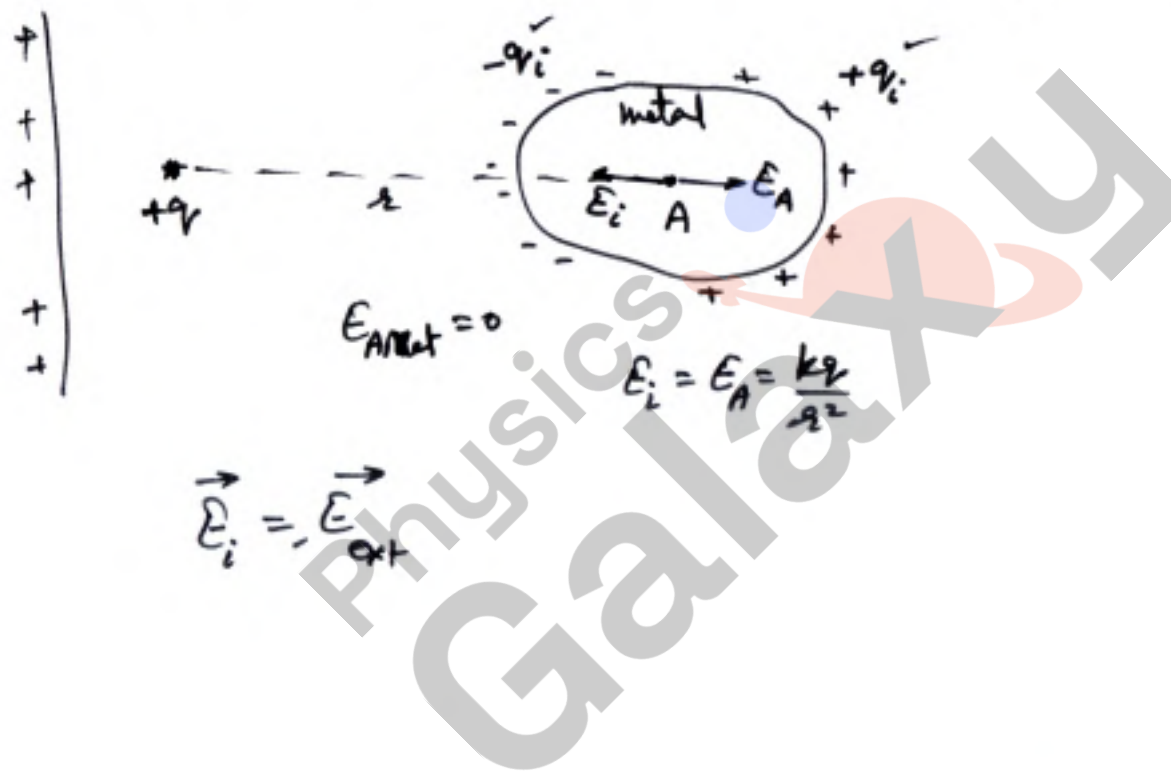
QUESTIONS BASED ON  
**# CONNECTING CONCENTRIC SHELLS**



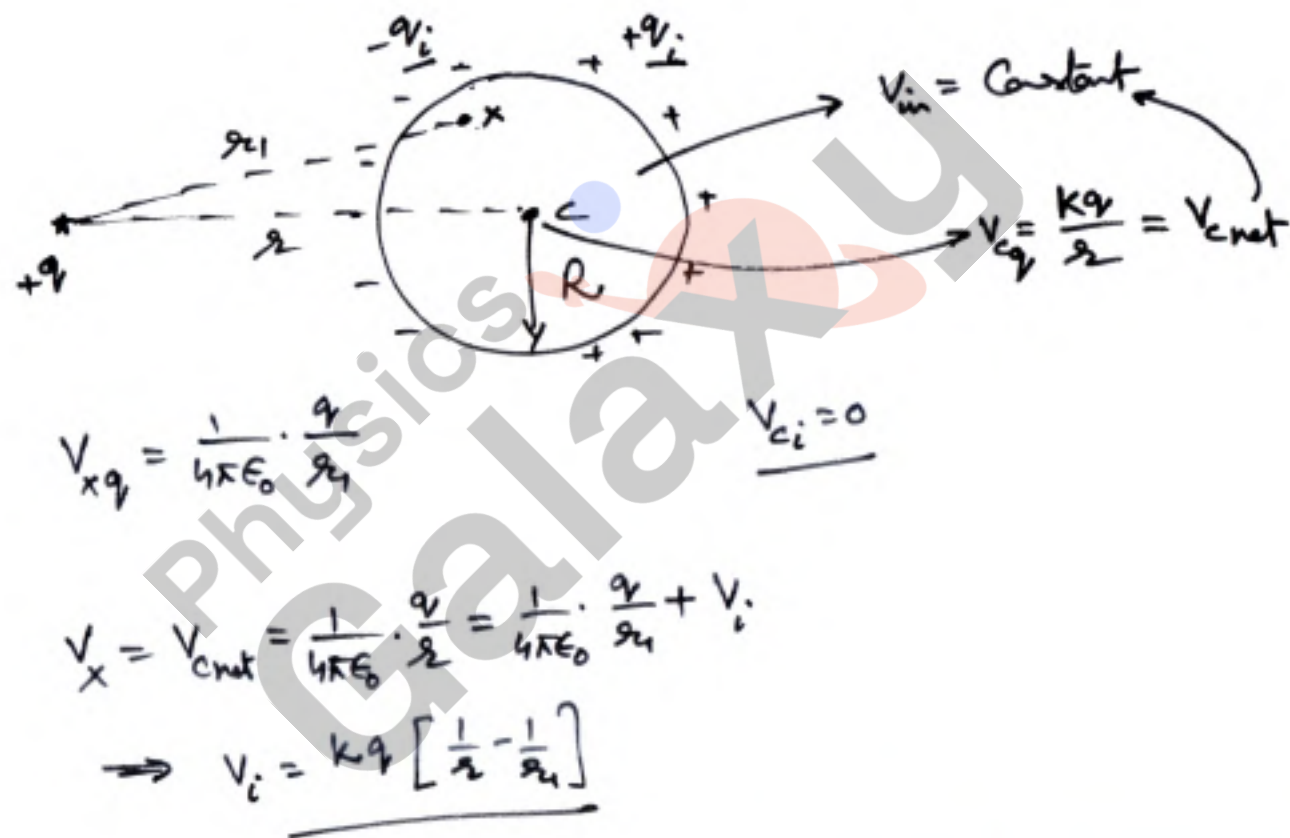
whole charge flows to outer shell



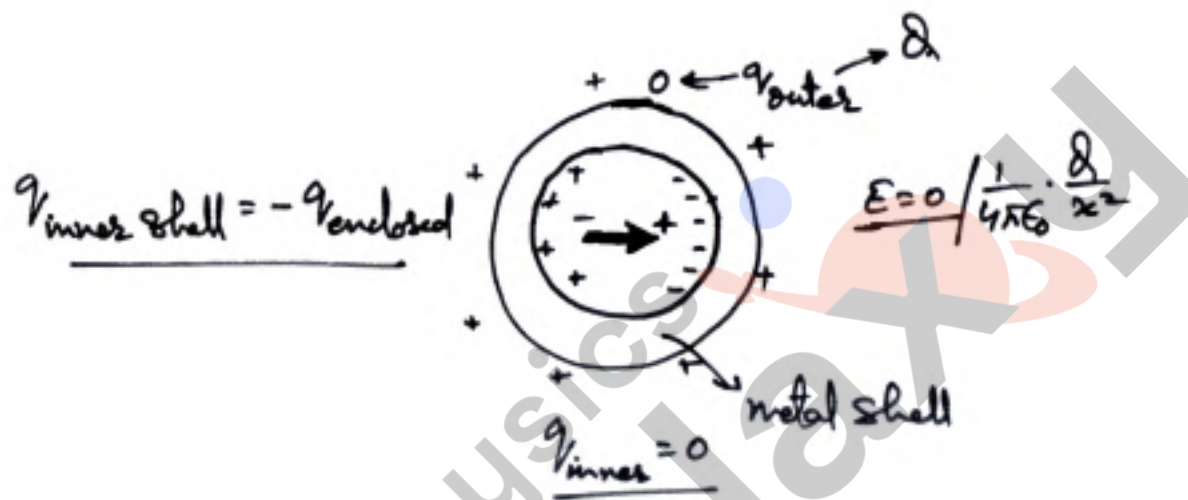
QUESTIONS BASED ON  
**# ELECTRIC FIELD DUE TO INDUCED CHARGES ON METAL BODY**



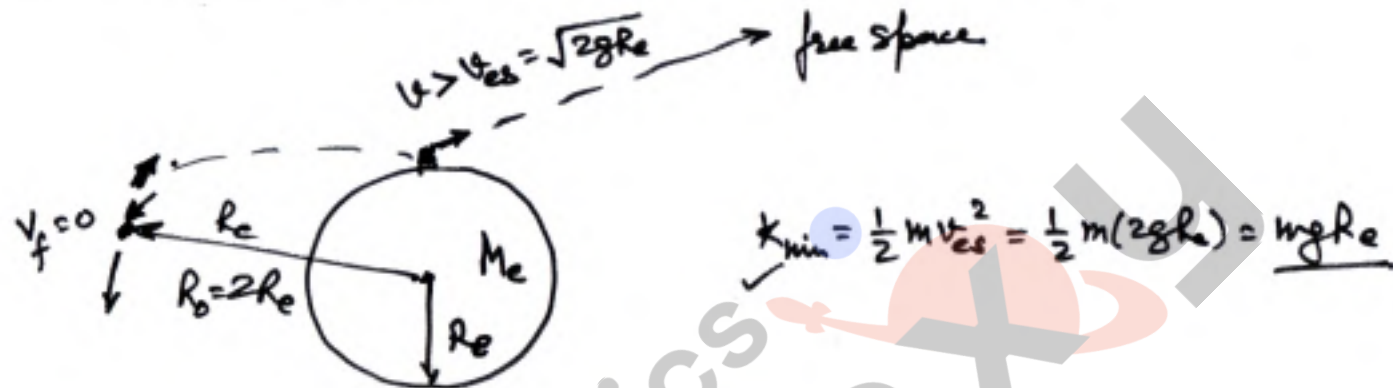
QUESTIONS BASED ON  
**# POTENTIAL DUE TO INDUCED CHARGES ON A METAL BODY**



QUESTIONS BASED ON  
# INDUCED CHARGES IN A SHELL DUE TO A DIPOLE



QUESTIONS BASED ON  
**# ENERGY REQUIRED TO LAUNCH A SPACESHIP**



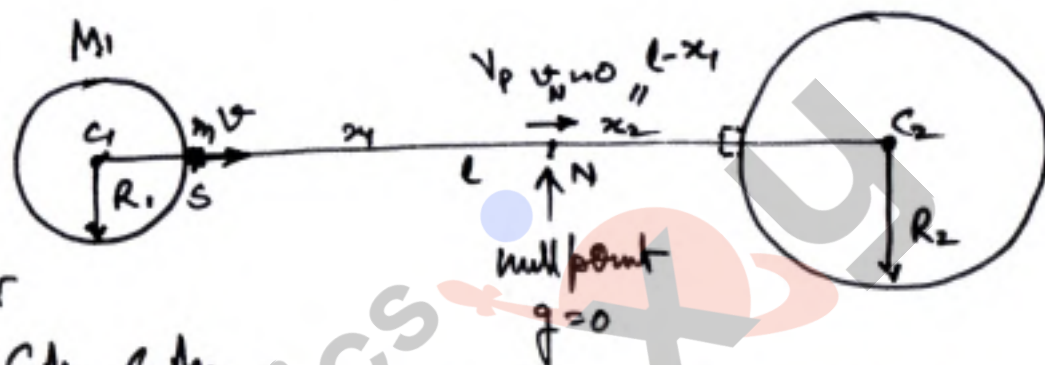
Energy reqd to raise the spaceship to  $R_0$ :

$$K_i + P_i = P_f$$

$$\frac{1}{2} m v^2 - \frac{G M_e m}{r_e} = - \frac{G M_e m}{R_0}$$

$$v = \dots$$

QUESTIONS BASED ON  
**# TRANSFERRING A BODY FROM ONE PLANET TO ANOTHER**



pot<sup>n</sup> of null pt

$$V_p = -\frac{GM_1}{x_1} - \frac{GM_2}{L-x_1}$$

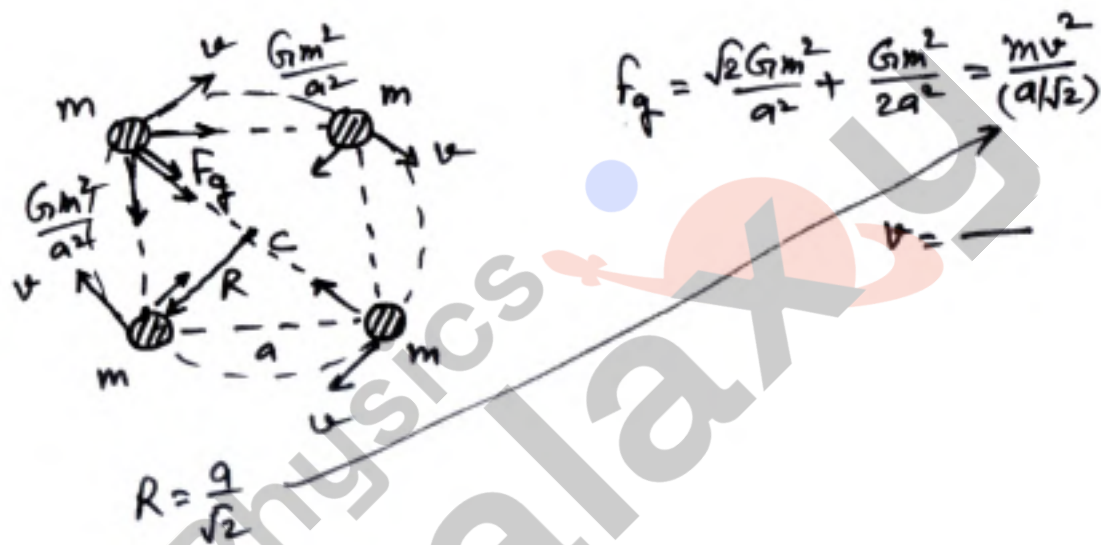
$$\frac{GM_1}{x_1^2} = \frac{GM_2}{(L-x_1)^2} \rightarrow x_1 = \dots$$

using energy cons from \$N\$

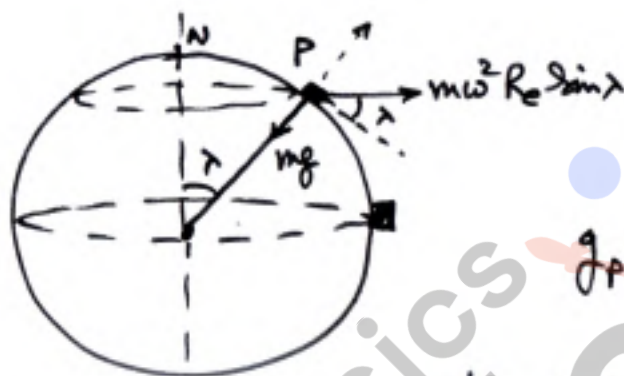
$$\frac{1}{2}mv^2 - \left( \frac{GM_1}{R_1} - \frac{GM_2}{L-R_1} \right) m = -mV_p$$

$$v = \dots$$

QUESTIONS BASED ON  
# REVOLUTION OF FOUR PARTICLES UNDER GRAVITATIONAL FORCE



QUESTIONS BASED ON  
**# EFFECT OF ROTATION OF EARTH ON WEIGHT OF BODIES**



$$g_P = g_E - \omega^2 R_e \sin^2 \lambda$$

if  $\omega_e \rightarrow 3\omega_e$   $\rightarrow$   $\omega_{\text{body at N}}$   $\rightarrow$   $3\omega_{\text{equate}}$

$$g_i = g_e - \omega^2 R_e$$

$$g_f = g_e - \underline{9\omega^2 R_e}$$

at a particular  $\lambda$ , we use

$$g_P = \frac{g_P}{5} = g - 9\omega^2 R_e \sin^2 \lambda$$


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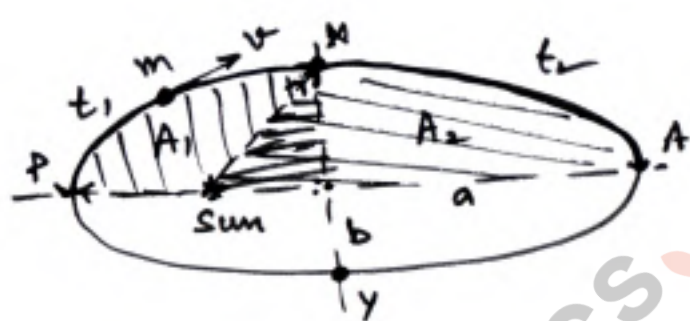
QUESTIONS BASED ON  
# PERIGEE & APOGEE RELATION IN ELLIPTICAL PATH



QUESTIONS BASED ON  
**# CHANGING ORBIT OF A SATELLITE IN ELLIPTICAL PATH**

$v_1 \leftarrow v_{10} = \sqrt{\frac{GM}{R_1}}$   
 $v_2 \rightarrow v_{20} = \sqrt{\frac{GM}{R_2}}$   
 $a = \frac{R_1 + R_2}{2}$   
 time of elliptical orbit  $T = \frac{4\pi^2}{GM} a^3$   
 time of orbit transfer  $t = T/2$   
 for elliptical path  
 $\left. \begin{aligned} \frac{1}{2} m v_1^2 - \frac{GMm}{R_1} &= \frac{1}{2} m v_2^2 - \frac{GMm}{R_2} \\ v_1 R_1 &= v_2 R_2 \end{aligned} \right\}$

QUESTIONS BASED ON  
**# TIME TO COVER AN ELLIPTICAL ARC BY A SATELLITE OR A PLANET**



Areal vel  $\rightarrow$  const

area of ellipse =  $\pi ab$

$$\frac{t_1}{t_2} = \frac{A_1}{A_2}$$

$$A_1 = \frac{\pi ab}{4} - A_T$$

$$A_2 = \frac{\pi ab}{4} + A_T$$

QUESTIONS BASED ON  
# ESCAPING OF A SATELLITE

$v_0 = \sqrt{\frac{GM}{r_2}}$

$v_{es} = \sqrt{2} v_0$

To free from gravity  
 $E_{ts} = 0$

$$\frac{1}{2} m v_{es}^2 - \frac{GMm}{r_2} = 0$$
$$v_{es} = \sqrt{\frac{2GM}{r_2}}$$

$\left( \frac{v_{es}}{v_0} = \sqrt{2} \right) \rightarrow \frac{1.414 v_0}{41.4\% \text{ inc.}}$